

1 **Spherule layers, crater scaling laws, and the population of ancient terrestrial**  
2 **impactors**

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17 **Keywords:** Cratering; Earth; Moon; Near-Earth objects; Planetary dynamics

18 **Abstract**

19 Ancient layers of impact spherules provide a record of Earth's early bombardment  
20 history. Here, we compare different bombardment histories to the spherule layer record  
21 and show that 3.2-3.5 Ga the flux of large impactors (10-100 km in diameter) was likely  
22 20-40 times higher than today. The E-belt model of early Solar System dynamics  
23 suggests that an increased impactor flux during the Archean is the result of the  
24 destabilization of an inward extension of the main asteroid belt (Bottke, W.F.,  
25 Vokrouhlický, D., Minton, D., Nesvorný, D., Morbidelli, A., Brasser, R., Simonson, B.,  
26 Levison, H.F., 2012. *Nature* 485, 78–81). Here, we find that the nominal flux predicted  
27 by the E-belt model is 7-19 times too low to explain the spherule layer record. Moreover,  
28 rather than making most lunar basins younger than 4.1 Gyr old, the nominal E-belt

29 model, coupled with a corrected crater diameter scaling law, only produces two lunar  
30 basins larger than 300 km in diameter. We also show that the spherule layer record when  
31 coupled with the lunar cratering record and careful consideration of crater scaling laws  
32 can constrain the size distribution of ancient terrestrial impactors. The preferred  
33 population is main-belt-like up to ~50 km in diameter transitioning to a steep distribution  
34 going to larger sizes.

35

## 36 **1. Introduction**

37 The constant recycling of Earth's crust by plate tectonics makes it impossible to use  
38 observations of terrestrial craters to determine if and how the impactor flux changed  
39 throughout Earth's history (Johnson and Bowling, 2014). Fortunately, very large impacts  
40 create distal ejecta layers with global extent (Smit, 1999). Even when the source crater  
41 has been destroyed, these layers can act as a record of the impacts that created them  
42 (Simonson and Glass, 2004). Although some impact ejecta layers are more proximal  
43 material transported as part of the ballistic ejecta curtain, many of the layers are distal  
44 deposits produced by impact (vapor) plumes (Glass and Simonson, 2012; Johnson and  
45 Melosh, 2014; 2012a; Simonson and Glass, 2004). Estimates of the size of the impactors  
46 that created these impact plume layers suggest that the impactor flux was significantly  
47 higher 2.4-3.5 Ga than it is today, although these flux estimates are mostly qualitative  
48 (Johnson and Melosh, 2012b).

49

50 The Early Archean to earliest Paleoproterozoic spherule layers formed well after the Late  
51 Heavy Bombardment (LHB) (because almost all the layers are Early or Late Archean in

52 age, we refer to them collectively as Archean from here on for the sake of convenience).  
53 The LHB is thought to have ended after the formation of the lunar basin Orientale, about  
54 3.7 Ga (Stöffler and Ryder, 2001). The Nice model is a dynamical model of the evolution  
55 of the orbits of the outer giant planets that has been used to explain the LHB through a  
56 destabilization of the main asteroid belt by abrupt migration of the giant planets (Gomes  
57 et al., 2005). The E-belt model, which includes an inward extension of the main asteroid  
58 belt from about 1.7-2.1 AU, was developed to explain the formation of the Archean  
59 spherule layers (Bottke et al., 2012).

60

61 Bottke et al. (2012) compare the expected number of Chicxulub-sized craters on Earth  
62 over the timespans where spherule-bearing sedimentary sequences have been found in the  
63 Archean. The E-belt model assumes 6 km diameter bodies striking at 22 km/s create  
64 “Chicxulub sized” (~160-km diameter) craters on Earth (Bottke et al., 2015). According  
65 to Johnson and Melosh (2012b), a 6-km diameter impactor would make a sparse spherule  
66 layer only 0.09-0.2-mm thick. However, the observed Archean spherule layers are  
67 centimeters to 10’s of centimeters thick and were likely created by impactors that are  
68 ~10-90 km in diameter (Johnson and Melosh, 2012b; Kyte et al., 2003; Lowe et al., 2003,  
69 2014; Lowe and Byerly, 2015). In section 2, using the method of Johnson and Melosh  
70 (2012b), we estimate the sizes of the impactors that created each of the Archean spherule  
71 layers. We then compare this record to different possible bombardment histories. We find  
72 that the nominal flux predicted by the E-belt model is 7-19 times too low to produce the  
73 Archean spherule layers.

74

75 In section 3 we show that careful application of crater scaling laws provides a reasonably  
76 consistent relationship (<10% discrepancy) between crater size and impactor properties  
77 that is in excellent agreement with recent numerical models of terrestrial crater formation.  
78 Then, as an additional test of the E-belt model, we calculate the impactor size required to  
79 produce a 160-km diameter “Chicxulub sized” crater on Earth. Contrary to the 6 km  
80 diameter impactor estimate of Bottke et al. (2012), a ~13 km diameter impactor is  
81 required to produce a 160-km diameter crater on Earth at an impact speed of ~22 km/s.  
82 The approximately factor of two discrepancy in impactor size implies that the Bottke et  
83 al. (2012) E-belt flux is overestimated by a factor of 7.5-10. In this scenario, the nominal  
84 E-belt model produces only two craters larger than 300 km in diameter on the Moon  
85 rather than most of the LHB basins (Bottke et al., 2012; Morbidelli et al., 2012).

86

87 Finally in section 4 we combine constraints on the impactor Size Frequency Distribution  
88 (SFD) with constraints from the lunar cratering record. We find that the population of  
89 ancient impactors that is roughly main-belt like from ~1-30 km in diameter but steeper  
90 than the main-belt SFD at larger sizes is consistent with the lunar cratering record and the  
91 terrestrial impact record from spherule layers.

92

## 93 **2. Spherule layer constraints on Terrestrial bombardment**

94 Observations of NEOs provide a direct estimate of the present-day impactor flux (Figure  
95 1; Stuart and Binzel, 2004). For objects greater than 10 km in diameter, these estimates  
96 suffer from small number statistics. Because asteroids larger than ~10 km in diameter are  
97 delivered to the NEO population predominantly by the size-independent effect of

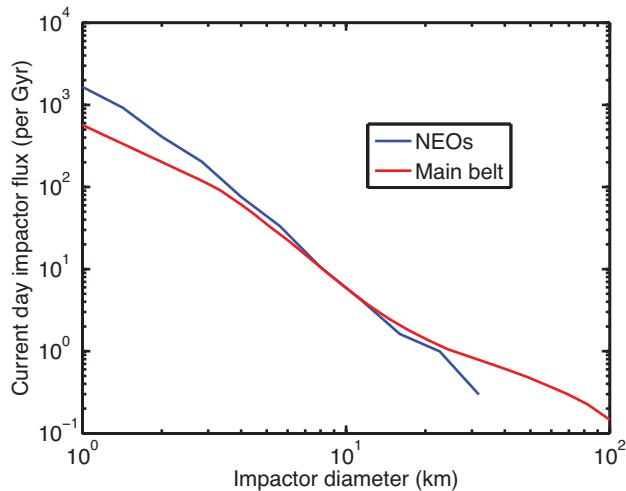
98 dynamical chaos, we expect little difference between NEO and main-belt size  
99 distributions for objects larger than 10 km in diameter (Minton and Malhotra, 2010).  
100 Thus, we scale the main-belt SFD (Minton et al., 2015b) to be equal to the NEO SFD for  
101 a 10-km diameter object (Figure 1). We then assume the actual current impactor flux is  
102 the maximum of these two curves, which is a similar method to that used by Le Feuvre  
103 and Wieczorek (2011). This combined impactor SFD allows us to compare different  
104 bombardment histories to the spherule layer record, which predicts some impactors were  
105 substantially larger than 30 km in diameter. We note that the size above which we expect  
106 the impactor SFD to appear main-belt like is not strictly constrained. Additionally, there  
107 is only a small size range where both distributions are well determined (ie. the main belt  
108 population is poorly constrained for bodies smaller than a few km in diameter while  
109 above a few km in size the NEO population suffers from poor statistics). However, the  
110 errors associated with flux estimates based on the spherule layer record are likely much  
111 larger than any uncertainty associated with our estimates of the current day impactor  
112 SFD.

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118 **Figure 1:** The cumulative rate of impacts larger than a given size as a function of  
 119 impactor diameter. The blue curve is the current impactor flux based on observations of  
 120 NEOs (Stuart and Binzel, 2004). We note that the impactor flux estimates of Stuart and  
 121 Binzel (2004) are in excellent agreement with more recent estimates in this size range  
 122 (Harris and D’Abramo, 2015). The red curve is the main belt asteroid belt size frequency  
 123 distribution (Minton et al., 2015b) scaled so that it is equal to the impactor flux of NEOs  
 124 for bodies with 10 km diameter.  
 125

126 Figure 2 shows the cumulative number of impacts by bodies larger than 10 km in  
 127 diameter for three bombardment histories. The decreasing flux estimate is based on  
 128 dynamical erosion of the asteroid belt (Minton and Malhotra, 2010) and is scaled so that  
 129 the current impactor flux is equal to the impactor flux calculated based on observations of  
 130 NEOs (Stuart and Binzel, 2004). One minor difference between this work and that of  
 131 Minton and Malhotra (2010) is that we have shifted the starting time of the decay of the  
 132 main asteroid belt from 4.0 Ga to 4.5 Ga. Because we normalize the flux rate so that the  
 133 current flux is equal to the estimates based on NEO observations, this change only  
 134 reduces the flux estimates by a factor of less than two during the times of interest. The  
 135 impact velocity of 22 km/s for E-belt impactors (Bottke et al., 2015; 2012) is not  
 136 significantly different from 20.3 km/s, the mean impact velocity of asteroids impacting  
 137 the Earth (Minton and Malhotra, 2010). According to Equation 1, this difference in

138 impact velocity only changes the transient crater size by 3.6%. Thus, we can safely  
139 ignore the slightly higher velocity of E-belt impactors and directly compare the number  
140 of impacting bodies of a given size when comparing different flux estimates.

141

142 The nominal E-belt model assumes that destabilization of the E-belt occurs 4.1 Ga,  
143 however, this timing is not strictly constrained (Bottke et al., 2012; Morbidelli et al.,  
144 2012). In the context of the Nice model, a destabilization of the E-belt 3.9 Ga  
145 corresponds to the lunar cataclysm view of the LHB, where almost all lunar basins  
146 formed about 3.9 Ga (Morbidelli et al., 2012). Moving the destabilization any later than  
147 that would imply that the Nice model cannot explain the LHB. Thus, we include flux  
148 estimates for destabilization at 4.1 Ga and 3.9 Ga to encompass the entire range of  
149 possible destabilization times (Figure 2).

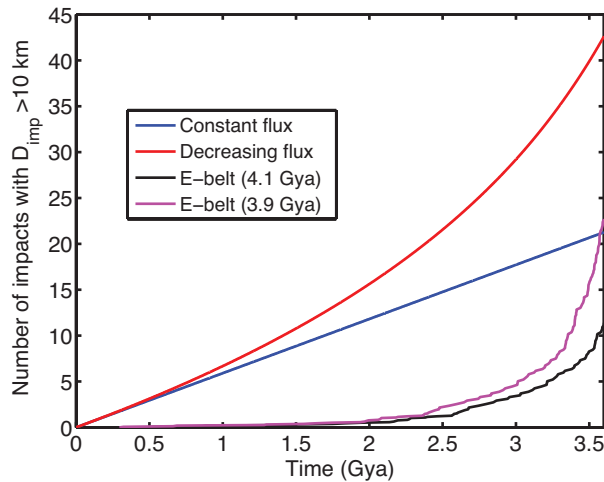
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156 **Figure 2:** Cumulative number of impactors larger than 10 km in diameter that hit the  
 157 Earth. The blue line is calculated assuming a constant impactor flux equal to the current  
 158 impactor flux (Stuart and Binzel, 2004). The red curve assumes the constantly decreasing  
 159 impactor flux estimated by Minton and Malhotra (2010). The flux rate from Minton and  
 160 Malhotra (2010) is normalized so that the current flux is equal to the estimates based on  
 161 NEO observations (Stuart and Binzel, 2004). The purple and black curves are the  
 162 cumulative number of “E-belt” impactors assuming a destabilization at 3.9 Ga and 4.1  
 163 Ga, respectively (Bottke et al., 2012). Note that the E-Belt impact curves were generated  
 164 using a very simple model for the migration of the giant planets, and therefore the decay  
 165 curves could potentially be different if a more realistic evolution of the outer planets were  
 166 considered. Note that including impacts out to 3.9 Gya, the cumulative bombardment  
 167 from the nominal E-belt model (purple) exceeds the the value implied by a decreasing  
 168 main belt flux (red) by a factor of 2.6.  
 169

170 As Table 1 shows, the age of the ancient spherule layers cluster between 2.49-2.63 Ga  
 171 and 3.23-3.47 Ga. To compare the flux to the number of spherule layers, we assume that  
 172 the clustering is purely the result of strata from these two periods being well searched and  
 173 particularly suited to preserving spherule layers. The average time between large impacts  
 174 is about 0.05 Gyr between 2.49-2.63 Ga and about 0.03 Gyr between 3.23-3.47 Ga. To  
 175 account in some crude way for the fact that impacts are Poisson distributed we add the  
 176 average recurrence rate to both sides of the respective period. More precisely we assume  
 177 the spherule layer record is complete between 2.44-2.68 Ga and 3.2-3.5 Ga. This means  
 178 that there may be several undiscovered, destroyed, or obscured layers that formed



179 between 2.68-3.2 Ga, but that we have found all of the layers that formed between 2.44-  
 180 2.68 Ga and 3.2-3.5 Ga. We note this assumption may produce a conservative estimate of  
 181 impactor flux because there may be more layers within the strata that have already been  
 182 searched. For example, Mohr-Westheide et al. (2015) and Koeberl et al. (2015a,b) report  
 183 on newly discovered Early Archean spherule layers in South Africa that may be distinct  
 184 from any of those previously reported by Lowe et al. (2003, 2014).  
 185

Name	Approximate age (Ga)	Aggregate thickness (cm)	Impactor Diameter (km)
Dales Gorge & Kuruman	2.49	0.5-6	11-39
Bee Gorge	2.54	1-3	13-31
Reivilo & Paraborndoo	2.54-2.56	2-2.5	17-29
Jeerinah, Carawine, & Monteville	2.63	0.4-30	10-67
S5	3.23	20-50	37-79
S4	3.24	12	31-49
S3	3.24	30	42-67
S2	3.26	10-70	29-88
S6	3.26-3.30	20-50	37-79
S8	3.30	20-50	37-79
S7	3.42	20-50	37-79
S1 & Warrawoona	3.47	5-6	23-39

186  
 187 **Table 1:** Archean spherule layers. The layer thickness and age estimates for S5-S8 come  
 188 from (Lowe et al., 2014) while all others are from Glass and Simonson (2012). The layers  
 189 with multiple names are layers found at multiple localities that were likely created by the  
 190 same impact (Glass and Simonson, 2012). For these “multiple” layers we report the entire  
 191 range of layer thicknesses. The aggregate thickness is an estimate of how thick a layer  
 192 composed of closely packed spherules would be. Aggregate thickness is the same as  
 193 reduced layer thickness used in (Johnson and Melosh, 2012b). The impactor diameter is  
 194 then calculated based on layer thickness using the same method as Johnson and Melosh  
 195 (2012b).  
 196  
 197

198 By convolving the cumulative number of impacts from Figure 2 with the assumed  
 199 probability of layer preservation and discovery, we can estimate the number of spherule

200 layers that a given bombardment history predicts. Note, the spherule layer record does  
201 not rule out a scenario where the impactor flux was high 2.44-2.68 Ga, low from 2.68-3.2  
202 Ga, and high from 3.2-3.5 Ga. However, such a bombardment history is inconsistent with  
203 any of the dynamical models we consider (Bottke et al., 2012; Minton and Malhotra,  
204 2010) and the terrestrial cratering record provides no evidence of periodic increases in  
205 impactor flux (Bailer-Jones, 2011). On shorter time scales, however, asteroid disruption  
206 events can produce increases in the flux of terrestrial impactors, as demonstrated by the  
207 formation of the Flora asteroid family, which has been linked to an increased impactor  
208 flux in the Ordovician (Nesvorný et al., 2007). It is unclear whether even larger  
209 disruption events could deliver enough material to explain the formation of the Archean  
210 spherule layers.

211

212 In Figure 3, we compare the flux implied by the four layers that formed 2.44-2.68 Ga to  
213 the various bombardment histories shown in Figure 2. Assuming the spherule layers are  
214 made by the smallest impactor sizes given in Table 1 and including the entire range of  
215 random variation implied by Poisson statistics (vertical error bars  $\sqrt{N}$ ), the spherule  
216 layers are consistent with all the bombardment histories in Figure 2 including a constant  
217 flux scenario. At the large end of the size range in Table 1, the spherule layers imply a  
218 flux from 2.44-2.68 Ga that is more than 10 times higher than the current impactor flux.  
219 At the low end of the size estimates from Table 1, however, the flux from 2.44-2.68 Ga is  
220 consistent with even the current day flux.

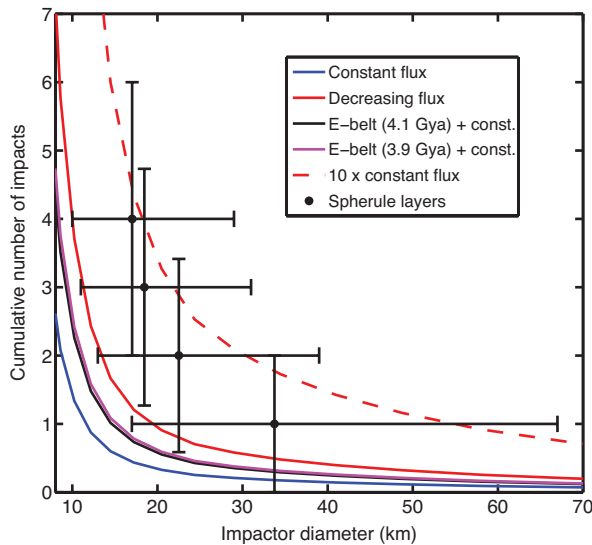
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222 In Figure 4, we compare the flux implied by the eight layers that formed 3.2-3.5 Ga to the  
223 various bombardment histories shown in Figure 2. We find the spherule layers are  
224 consistent with a flux significantly higher than any bombardment history in Figure 4.  
225 Assuming the destabilization of the E-belt occurred at 4.1 Ga the E-belt flux during the  
226 time of spherule layer formation is 2.1 times the current impactor flux. Note that E-belt  
227 flux refers to the flux of impactors from the extension of the asteroid belt alone as shown  
228 in Figure 2. Assuming the E-belt model is correct, the E-belt flux is in addition to some  
229 background flux of material coming from the main belt. In Figures 3 and 4 we plot the  
230 sum of the E-belt flux and the constant flux model. In the text however, we also consider  
231 adding the E-belt flux to the decreasing flux of Minton and Malhotra (2010). If we  
232 instead assume the E-belt destabilized 3.9 Ga, the E-belt flux is 5.1 times higher than the  
233 current impactor flux during the period of spherule layer formation. The average flux  
234 from the decreasing flux model is 5.8 times the constant flux model. We find that a total  
235 impactor flux that is ~20-40 times the current, constant, impactor flux is required to  
236 explain the Archean Spherule layers (dashed lines; Figure 4). We note the SFD inferred  
237 from the spherule layers looks different from that of the main belt; we will return to this  
238 in section 4.

239

240 Assuming the flux from the main belt is given by the constant flux model, the E-belt flux  
241 would need to be 19-39 times the current impactor flux from 3.2-3.5 Ga to produce the  
242 spherule layers that formed during this period. This corresponds to 9.0-19 times the E-  
243 belt flux assuming destabilization occurred 4.1 Ga and 3.7-7.6 times if destabilization  
244 occurred 3.9 Ga. If instead we assume the flux from the main belt is given by the

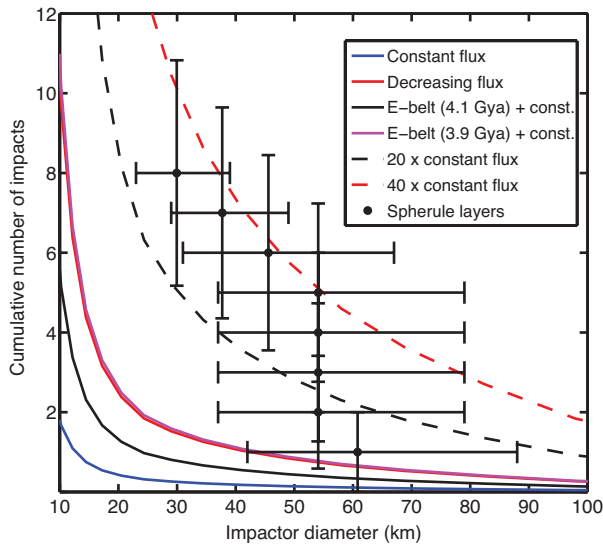
245 decreasing flux of Minton and Malhotra (2010), the E-belt flux would need to be 14-34  
 246 times the current current impactor flux from 3.2-3.5 Ga to produce the spherule layers  
 247 that formed during this period. This corresponds to 6.7-16 times the E-belt flux assuming  
 248 destabilization occurred 4.1 Ga and 2.7-6.7 times if destabilization occurred 3.9 Ga. The  
 249 Hungaria asteroids are thought to be the only survivors of the E-belt (Bottke et al., 2012).  
 250 Because the current population of Hungarias is so small, statistics allow an E-belt flux  
 251 that was a factor of two higher than the nominal case (Bottke et al., 2012). Even with a  
 252 doubling in flux, the E-belt flux is too low to explain the formation of the Archean  
 253 spherule layers.



254

255 **Figure 3:** Cumulative number of impacts larger than a given size plotted as a function of  
 256 impactor diameter. The curves all represent the number of impacts between 2.44-2.68 Ga  
 257 predicted by different dynamical models as indicated by the legend. The black and purple  
 258 curves are the cumulative number of impacts from the E-belt added to the number  
 259 expected from the constant flux scenario. The points with error bars represent the range  
 260 of SFDs allowed by the spherule layer data from Table 1. The horizontal error bars  
 261 connect the two SFDs assuming the minimum and maximum size estimates in Table 1.  
 262 The vertical error bars assume Poisson statistics ( $1-\sigma$  error of  $\sqrt{N}$  where  $N$  is the number  
 263 of layers). Although these errors should technically be on the flux estimates they provide  
 264 a sense of the ranges of impactor flux that could explain the abundance of spherule  
 265 layers.

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**Figure 4:** Cumulative number of impacts larger than a given size plotted as a function of impactor diameter. The curves all represent the number of impacts between 3.2-3.5 Ga predicted by different dynamical models as indicated by the legend. The black and purple curves are the cumulative number of impacts from the E-belt added to the number expected from the constant flux scenario. The points with error bars represent the range of SFDs allowed by the spherule layer data from Table 1. The horizontal error bars connect the two SFDs assuming the minimum and maximum size estimates in Table 1. The vertical error bars assume Poisson statistics ( $1-\sigma$  error of  $\sqrt{N}$  where  $N$  is the number of layers). Although these errors should technically be on the flux estimates they provide a sense of the ranges of impactor flux that could explain the abundance of spherule layers.

### 282 3 Crater scaling laws

283 A principal constraint used to test any impact flux model is the observed number of  
284 impact basins on Earth and the Moon. For example, Bottke et al. (2012) used the  
285 observed number of post-LHB “Chicxulub-scale” ( $D > 160$  km) impact craters on Earth  
286 and the Moon as a test of their E-belt impact flux model. Crucially, to convert a  
287 theoretical impactor SFD into a crater SFD requires a recipe for predicting the size of the  
288 final crater formed by the collision of an impactor of known mass, velocity and angle

289 onto a planetary surface of known density and gravity. While this procedure is  
290 straightforward for small, simple bowl-shaped craters, it is complicated greatly by the  
291 process of crater modification (collapse) that becomes increasingly prevalent as crater  
292 size increases and internal crater morphology departs more and more from a simple bowl.  
293 As a result, several frameworks have been described and used in the literature, based on  
294 different observational constraints and assumptions about the nature of crater collapse, to  
295 predict the amount of enlargement that occurs during crater modification. While  
296 misapplication of these different approaches provides scope for disparate results, here we  
297 show that their careful application provides a reasonably consistent relationship (<10%  
298 discrepancy) between crater size and impactor properties that is in excellent agreement  
299 with recent numerical models of terrestrial crater formation. In section 5, we apply this  
300 framework to compare the flux inferred from spherule layers to the lunar cratering record.

301

302 Estimating crater size from impactor and target properties is conventionally done in two  
303 steps. First, equations derived using the point-source approximation and dimensional  
304 analysis relate impactor and target properties to the diameter of the so-called transient  
305 crater (Holsapple, 1993; Holsapple and Schmidt, 1982). These equations are constrained  
306 by laboratory-scale impact experiments (Schmidt and Housen, 1987) and numerical  
307 models. As its name indicates, the transient crater is the short-lived bowl-shaped cavity  
308 excavated during the early stages of impact, which is modified by gravity-driven collapse  
309 of the transient crater walls and floor.

310

311 The diameter of the transient crater,  $D_{trans}$ , measured at the pre-impact target surface, is  
312 given by the following equation from Collins et al. (2005) and references therein:

$$313 \quad D_{trans} = 1.161 \left( \frac{\rho_{imp}}{\rho_{targ}} \right)^{\frac{1}{3}} D_{imp}^{0.78} v_{imp}^{0.44} g^{-0.22} \sin^{1/3}(\theta), \quad (1)$$

314 where  $\rho_{imp}$  is impactor density,  $\rho_{targ}$  is target density,  $D_{imp}$  is impactor diameter,  $v_{imp}$   
315 is impact velocity,  $g$  acceleration due to gravity, and  $\theta$  is the impact angle measure with  
316 respect to the target surface ( $90^\circ$  for a vertical impact and  $0^\circ$  for a grazing impact). All of  
317 the quantities in Equation 1 are in MKS units. This equation is valid for gravity-scaled  
318 craters, meaning the weight of the excavated material is the principal force arresting  
319 crater growth. On Earth, Equation 1 is valid for impactors larger than about one meter in  
320 diameter (Holsapple, 1993). This equation also assumes the impact is into a target with  
321 no appreciable porosity. We note again that the impactor size, velocity and gravity  
322 dependencies (exponents) in this equation are constrained by laboratory-scale impact  
323 experiments (e.g., Schmidt and Housen, 1987).

324

325 The transient crater diameter is not equal to the final crater diameter. The bowl-shaped  
326 transient crater is unstable and collapses under the influence of gravity. Scaling from  
327 transient crater to final crater size is not experimentally constrained. On Earth, craters  
328 larger than  $D_{sc} \approx 2 - 4$  km have more complex morphologies, including central uplifts  
329 and peak rings. These morphologies are attributed to uplift of the crater floor during wall  
330 collapse (e.g., Melosh, 1989). Several scaling laws based on detailed observation of  
331 craters and their ejecta, as well as reconstructions of transient crater geometry, have been  
332 used to produce relationships between transient crater and final crater diameter (Croft,  
333 1985; Holsapple, 1993; Schenk and McKinnon, 1985). Correct application of these

334 expressions requires careful attention to the definitions of pre- and post-collapse crater  
335 diameters, measured either at the level of the pre-impact surface or at the crater rim. As  
336 Equation (1) defines the diameter at the pre-impact level, here we take care to relate that  
337 measure of the transient crater ( $D_{trans}$ ) to the final crater diameter measured at the rim  
338 crest ( $D_{final}$ ). The increase in crater diameter therefore results from both crater  
339 enlargement by rim collapse and the inward-dipping slope of the rim.

340

341 Grieve and Garvin (1984) describe a well-tested geometric model for the collapse of  
342 simple craters. This model, under the assumption of a 5-10% increase in the volume of  
343 the collapsing rim material to account for shear bulking, suggests that the ratio  $\gamma = \frac{D_{final}}{D_{trans}}$   
344 (the final crater diameter measured at the rim crest divided by the transient crater  
345 diameter measured at the pre-impact level) is 1.23-1.28. This brackets the  $\gamma = 1.25$   
346 assumed by Collins et al. (2005).

347

348 Several authors (e.g., Croft, 1985; Schenk and McKinnon, 1985, Holsapple, 1993)  
349 describe similar geometric models for complex crater formation. To combine with  
350 Equation (1), these equations should take the general form:

$$351 \quad D_{final} = AD_{sc}^{-\eta} D_{trans}^{1+\eta} \quad (2)$$

352 where  $D_{sc}$  is the final rim diameter at the simple-to-complex transition and  $A$  and  $\eta$  are  
353 constants. However, to compare these models it is crucial that a consistent definition of  
354  $D_{trans}$  is used. Although these equations all seek to relate final crater diameter to  
355 transient crater diameter they are most informatively compared when expressed in the  
356 form:



357 
$$\frac{D_{final}}{D_{eqs}} = \left(\frac{D_{eqs}}{D_{sc}}\right)^\eta \quad (3)$$

358 where  $D_{sc}$  is the final rim diameter at the simple-to-complex transition,  $D_{eqs} = \gamma D_{trans}$  is  
 359 the final rim diameter of the “equivalent simple crater” and  $\eta$  is the same constant as in  
 360 Equation (2). This form is convenient because the enlargement factor is 1 at the simple-  
 361 to-complex transition and increases monotonically as crater size increases (the equation  
 362 does not apply for  $D_{eqs} < D_{sc}$ ). When expressed in this form, the three geometric models  
 363 of complex crater collapse in wide use can be described by  $\eta$  and  $\gamma = A^{\frac{1}{1+\eta}}$ , the ratio of  
 364 final to transient crater diameter for simple craters (Table 2).

365

366 Table 2 Complex crater enlargement model parameters

Model	$\eta$	$A$	$\gamma$
Croft (1985)	<b>0.123-0.234</b>	<b>1</b>	1
Croft (1985); modified	<b>0.123-0.234</b>	1.28-1.32	<b>1.25</b>
Schenk and McKinnon (1985) <sup>1</sup>	<b>0.13</b>	<b>1.17</b>	1.15
“ modified	<b>0.13</b>	1.29	<b>1.25</b>
Holsapple (1993)	<b>0.086</b>	1.35	<b>1.32</b>

367 Bold values are specified; remaining parameter is implied.

368 <sup>1</sup>Description of the Schenk and McKinnon (1985) model is also presented in McKinnon  
 369 and Schenk (1985) and McKinnon et al. (2003).

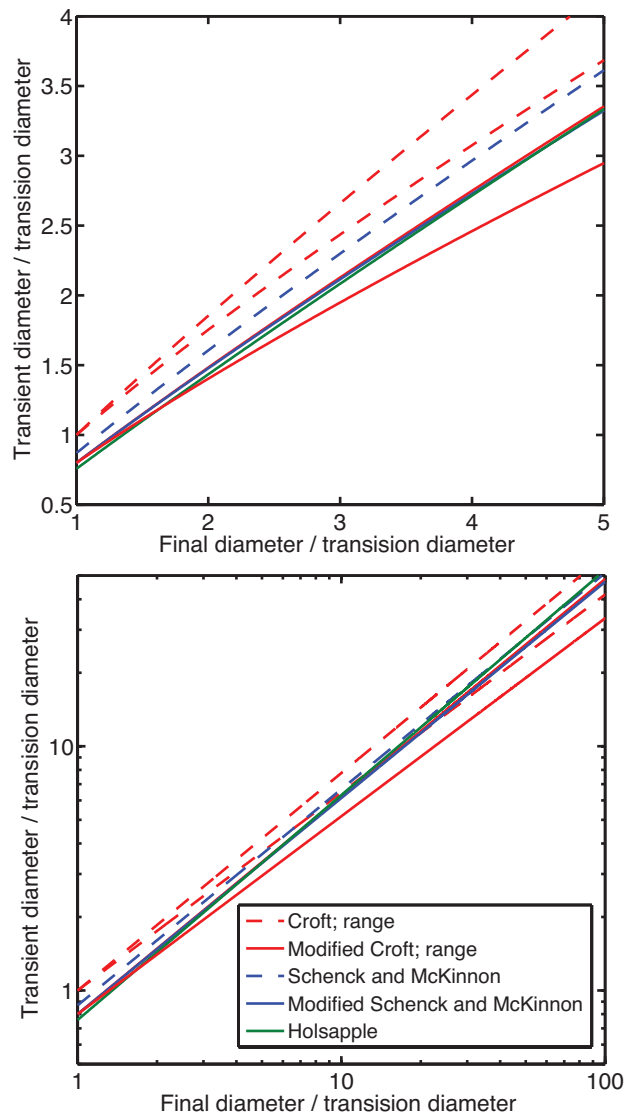
370

371 A comparison of the complex crater collapse models of Croft (1985), Schenk and  
 372 McKinnon (1985) and Holsapple (1993) reveals that they (apparently) make quite  
 373 disparate assumptions regarding crater enlargement for craters with diameters below the  
 374 simple-complex transition, ranging from  $\gamma = 1$  (i.e., no collapse; Croft, 1985) to  $\gamma =$

375 1.32 (Holsapple, 1993). The assumption of  $\gamma = 1$  is not appropriate for two reasons.  
376 First, both geometric and numerical models of simple crater formation show that  
377 substantial enlargement occurs in large simple craters via debris sliding of the over-  
378 steepened transient crater rim walls. Second, a value of  $\gamma = 1$  only makes sense if the  
379 transient crater diameter is measured at the rim; according to the transient crater diameter  
380 definition preferred here,  $\gamma$  must be 5-10% larger to account for the slope of the transient  
381 crater rim above the preimpact surface. This latter observation also applies to the value of  
382  $\gamma = 1.15$  adopted by Schenk and McKinnon (1985), because they also defined the  
383 transient crater diameter at the transient crater rim. In this case, the implied value of  $\gamma$ , as  
384 defined here, would be about  $\approx 1.24$  (Figure 7 in Schenk and McKinnon, 1985). To  
385 adjust both of these models to use transient crater diameter at the pre-impact level (and  
386 account for simple crater collapse) we have redefined the value of  $A$  in Equation (2) for  
387 each model assuming  $\gamma = 1.25$ , as suggested by the geometric model of simple crater  
388 collapse proposed by Grieve and Garvin (1984) (modified model parameters in Table 2).  
389 We note that as this modification leaves Equation (3) unchanged, it has no consequence  
390 for how each model was derived from observations. Holsapple (1993) based his  
391 assumption of  $\gamma = 1.32$  (which adopts the same transient crater diameter definition as  
392 used here) on measured shapes and rim profiles of craters produced in small-scale  
393 laboratory cratering experiments, which are often regarded as “frozen” transient craters.  
394 Although this is somewhat larger than 1.25 it has a sound basis and serves as a useful  
395 measure of uncertainty in simple crater enlargement. We therefore retain it for our  
396 analysis rather than modifying it to assume a consistent value of  $\gamma$  across all (modified)  
397 models.

398

399 Figure 5 compares the five complex crater collapse models given by Equation 2 and  
400 parameters in Table 2. Both transient and final crater diameters are normalized to the  
401 simple-complex transition diameter  $D_{sc}$ . There is good agreement between the three  
402 modified models (solid lines) if the lower bound for complex crater enlargement of Croft  
403 (1985) is used. Adopting the upper bound of Croft (1985) would overestimate the final  
404 crater diameter by as much as 60% if that model was applied to the largest lunar basins.  
405 Also evident is the potential for a systematic discrepancy between models of ~30% in  
406 final crater diameter if inconsistent definitions of the transient crater diameter are used.



407  
 408 **Figure 5** Comparison of complex crater enlargement scaling laws. Transient crater  
 409 diameter normalized by the simple-complex transition diameter as a function of final  
 410 (rim) diameter normalized in the same way. Dashed lines show the original models of  
 411 McKinnon and Schenk (1985) and Croft (1985) in which the transient crater diameter is  
 412 measured at the rim. Solid lines show the modified models in which transient crater  
 413 diameter is measured at the pre-impact level, for use with transient crater scaling laws.  
 414

415 Another way to estimate final crater diameters is using detailed numerical models called  
 416 hydrocodes or shock physics codes to directly model crater excavation and collapse. The  
 417 iSALE shock physics code has been rigorously tested against experiment including  
 418 impact and shock experiments in porous materials (Collins et al., 2011; Wünnemann et

419 al., 2006); oblique impact experiments into strong ductile materials (Davison et al.,  
420 2011); and thin plate jetting experiments (Johnson et al., 2014). The iSALE shock  
421 physics code includes detailed constitutive relations used to model the deformation of  
422 geologic materials (Collins et al., 2004). Recently Collins (2014) added a dilatancy  
423 model, which describes how deformation increases the porosity of geological materials.  
424 Using iSALE Collins (2014) modeled the formation of terrestrial craters from roughly 2-  
425 200 km in diameter by varying impactor diameter from 0.1-20 km in diameter. In  
426 addition to matching the observed morphology of craters including the transition from  
427 simple to complex craters and the transition from central-peak to peak-ring craters, these  
428 models also reproduced the observed gravity signature of terrestrial craters (Collins,  
429 2014).

430

431 Figure 6 shows a comparison between the crater diameter predicted by scaling laws,  
432 (Equations 1 and 2), and the model crater diameters from Collins (2014). The scaling law  
433 for transient crater size (Equation 1) is derived from impact experiments and the scaling  
434 laws for final crater diameter (Equation 2) are derived from observation of craters and  
435 their ejecta, as well as reconstructions of transient crater geometry. Thus numerical  
436 models of crater formation and collapse act as an independent test of these scaling laws.  
437 We determine the rim location from the models by measuring the point of highest  
438 topography, measured with respect to the pre-impact surface. As rim topography tends to  
439 be smooth in the numerical simulations, introducing a small uncertainty in the exact rim  
440 location, the error bars in Figure 6 represent the innermost and outermost location where

441 the crater reaches 90% of this highest topography. Clearly, the simple scaling laws and  
442 detailed models of crater formation are in excellent agreement.

443

444 Given the close correspondence between the numerical impact models and the (modified)  
445 complex crater collapse scaling laws, and the consistency between scaling laws,  
446 particularly those of Croft (1985; lower bound) and Schenk and McKinnon (1985), we  
447 propose that the latter model be used to derive an equation for general use that relates  
448 impactor and target properties directly to the final crater rim diameter by combining Eqs  
449 1 and 2:

$$450 \quad D_{fin} = 1.52 \left( \frac{\rho_{imp}}{\rho_{targ}} \right)^{0.38} D_{imp}^{0.88} v_{imp}^{0.5} g^{-0.25} D_{SC}^{-0.13} \sin^{0.38}(\theta) \quad (4)$$

451 All of the quantities in Equation 4 are in MKS units. Note that the value for the simple to  
452 complex transition  $D_{SC}$  is target body specific and that Equation 4 is only valid for final  
453 craters larger than  $D_{SC}$ . We note that the ~10% difference between various scaling laws  
454 and numerical models (figure 6) can be used as a rough estimate of the error associated  
455 with equation 4.

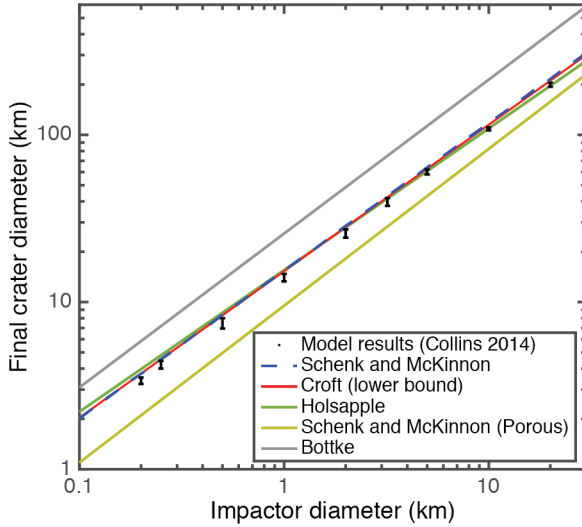
456

457 Figure 6 shows that craters formed in non-porous targets are larger than those that form  
458 in porous targets. Producing a good match between observed sizes of lunar craters and  
459 the current day population of impactors, based on observations of NEOs and the main  
460 asteroid belt, requires a transition from porous scaling to non-porous scaling at a crater  
461 size around 0.5-10 km in diameter (Ivanov and Hartmann, 2007). Although, this does not  
462 affect our estimates of the impactor sizes needed to create large craters, for completeness  
463 we create an equation for final crater diameter that is appropriate for impacts into porous

464 targets. This equation uses the modified Schenk and McKinnon (1985) for transient to  
 465 final crater scaling.

$$466 \quad D_{fin} = 1.66 \left( \frac{\rho_{imp}}{\rho_{targ}} \right)^{0.38} D_{imp}^{0.94} v_{imp}^{0.38} g^{-0.19} D_{sc}^{-0.13} \sin^{0.38}(\theta) \quad (5)$$

467



468

469

470 **Figure 6:** Comparison of numerical impact models and crater scaling laws. The solid  
 471 curves were calculated using Equations 1 and 2, with parameters in Table 1, using the  
 472 same impact conditions as those of the numerical impact models of Collins (2014),  
 473  $v_{imp} = 15$  km/s,  $\rho_{imp} = \rho_{targ}$ ,  $\theta = 90^\circ$ ,  $g = 9.81$  m/s<sup>2</sup>, and  $D_{sc} = 4$  km. The points  
 474 with error bars are the final crater diameters, for craters larger than  $D_{sc}$ , from Collins  
 475 (2014). The main text describes how rim location and error bars are determined. The red  
 476 curve shows the results obtained using the equations from the LPL calculator (equations  
 477 described in text) and assuming, as Bottke et al. (2012, 2015) do, that an impactor of a  
 478 given size produces a crater of the same size on both the Earth and the Moon. That is,  
 479  $v_{imp} = 15$  km/s,  $\rho_{imp} = \rho_{targ}$ ,  $\theta = 90^\circ$ ,  $g = 1.67$  m/s<sup>2</sup>,  $D_{sc} = 18$  km.  
 480

480

481 For a typical E-belt impact with  $v_{imp} = 22$  km/s,  $\rho_{imp} \approx \rho_{target}$ ,  $D_{sc} = 4$  km, and the  
 482 most probable impact angle  $\theta = 45^\circ$ , a 13.2-km diameter impactor is required to make a  
 483 Chicxulub-sized crater,  $D_{final} = 160$  km, on Earth. This impactor diameter is more than  
 484 a factor of two larger than that assumed to produce Chicxulub-sized craters in tests of the

485 E-belt model (Bottke et al., 2012; 2015). E-belt impactors were initially assumed to have  
486 a SFD similar to the current main belt (Bottke et al., 2012; Minton et al., 2015b). Using  
487 the SFD of the main belt (Figure 1), we compare the number of 6 km diameter bodies to  
488 the number of 13.2-km diameter bodies. We find that the E-belt forms 71 craters larger  
489 than 160 km in diameter on Earth over 4.1 Gyr where Bottke et al. (2012) report that 523  
490 should form. Thus, the E-belt model overstates its consequences by a factor of more than  
491 7.4. If instead we assume E-belt impactors had a SFD similar to Near Earth Objects  
492 (NEOs), the same comparison indicates this factor is 9.7.

493

494 For the same impact conditions above, we find a 27-km diameter impactor is required to  
495 form a 300-km diameter impact basin on Earth. Using the SFD of the main belt, we  
496 compare the number of 6-km diameter bodies to the number of 27-km diameter bodies.  
497 We find that the E-belt creates 22 basins larger than 300 km in diameter on Earth over 4.1  
498 Gyr where Bottke et al. (2012) reports that 154 such basins should form.

499

500 Using Equation 4 with lunar gravity  $g = 1.62 \text{ m/s}^2$ ,  $D_{SC} = 15 \text{ km}$  appropriate for the  
501 Moon (Croft, 1985),  $v_{imp} = 22 \text{ km/s}$ ,  $\rho_{imp} \approx \rho_{target}$ , and the most probable impact  
502 angle  $\theta = 45^\circ$ , we find 9.7-km and 19.7-km diameter impactors are required to create  
503 160-km and 300-km craters on the Moon, respectively. Using the main-belt SFD we  
504 compare the number of 6-km diameter bodies to the number of 9.7-km and 19.7-km  
505 diameter bodies. We find that the nominal E-belt model only creates 2 lunar craters larger  
506 than 300 km and 8.7 craters larger than 160 km in diameter in 4.1 Gyr compared to the  
507 9.1 and 31 reported by Bottke et al. (2012), respectively.



508

509 Bottke et al. (2012; 2015) use the following LPL online calculator to estimate final crater  
510 diameter produced by a given impact (<http://www.lpl.arizona.edu/tekton/crater.html>). The  
511 source code reveals that the calculator uses Equation 1 to calculate the transient crater  
512 diameter but the final crater diameter is calculated using  $D_{final} = D_{eqs}^{1.18} / D_{SC}^{0.18}$  (Croft,  
513 1985), where the equivalent simple crater diameter is assumed to be  $D_{eqs} = 1.56 D_{trans}$   
514 (i.e.,  $\gamma = 1.56$ ). Hence, this approach overestimates both the enlargement factor owing to  
515 simple crater collapse ( $\gamma$ ) and the additional enlargement owing to complex crater  
516 collapse (through the exponent  $\eta$ ). Another minor effect that contributes to the  
517 overestimate of crater sizes in Bottke et al. (2012; 2015) is the assumption that an  
518 impactor of a given size makes a crater of the same size on both the Earth and the Moon.  
519 More precisely, Bottke et al. (2012; 2015) use  $g = 1.67 \text{ m/s}^2$  and  $D_{SC} = 18 \text{ km}$  for both  
520 the Earth and Moon.

521

522 Johnson and Bowling (2014) estimated the expected terrestrial cratering record based on  
523 different terrestrial bombardment histories. They reported that the impactors from the E-  
524 belt alone could create six craters larger than 85 km in diameter that may have survived  
525 until today (Johnson and Bowling, 2014). Unfortunately, Johnson and Bowling (2014)  
526 assumed that the number of Chicxulub-sized craters the E-belt can form reported by  
527 Bottke et al. (2012) was correct. Thus, they overestimate the contribution of the E-belt to  
528 the terrestrial cratering record by a factor of 7.5-10. Considering this, we conclude that  
529 the nominal E-belt would at most create a single crater larger than 85 km in diameter that  
530 survives to the current day on Earth. At least 6 craters of this size have been recognized

531 on Earth. Because Bottke et al. (2012) did not report the impactor diameter assumed to  
532 make Chicxulub-sized craters, any paper using their flux estimates likely overestimates  
533 the E-belt flux by a factor of ~7.5-10.

534

#### 535 **4 The size distribution of ancient terrestrial impactors**

536 We have assumed that the SFD of impactors that created the spherule layers was  
537 equivalent to the main belt SFD. However, recent work shows that bombarding the Moon  
538 with a main-belt-like SFD would create an overabundance of mega-basins, craters with  
539 diameters greater than 1200 km (Minton et al., 2015b). An impactor SFD that agrees with  
540 the lunar cratering record has ~630 impactors larger 5.5 km in diameter for every one  
541 impactor larger than 70 km in diameter (Minton et al., 2015b). Two scenarios that adhere  
542 to this constraint are shown by the grey diamonds (scenario 1) and blue squares (scenario  
543 2) in Figure 7. We propose two potential SFDs that are consistent with both the lunar  
544 cratering record and the spherule layer record. These SFDs also minimize differences  
545 between the proposed SFDs and the main-belt SFD.

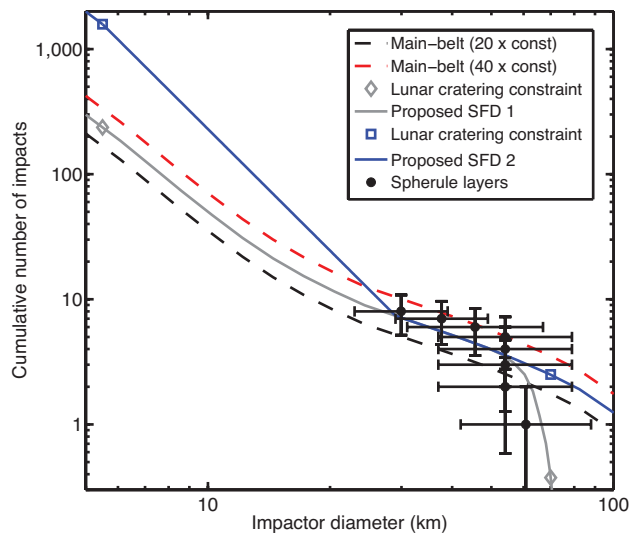
546

547 The grey “Proposed SFD 1” curve in Figure 7 shows a SFD that is main-belt-like up to  
548 ~50 km in diameter with an abrupt steepening above 50 km. This SFD is similar to the  
549 SFDs produced by catastrophic disruption of large parent bodies (Durda et al., 2007). In a  
550 catastrophic disruption SFD the steepening occurs at diameters near the largest remaining  
551 fragment size (Durda et al., 2007). This does not match the predictions of the E-belt  
552 model (Bottke et al., 2015; 2012), but is potentially consistent with a giant impact ejecta  
553 origin for the LHB impactors and the impactors that created the Archean spherule layers

554 (Minton et al., 2015a; Volk and Gladman, 2015). Although Figure 3 only includes  
555 spherule layers corresponding to impactors that are ~20-30 km in diameter, figure 4  
556 includes spherule layers that correspond to impactors that are ~30-60 km in diameter (ie.  
557 the same size range where proposed SFD 1 becomes steep). The impactor SFD from  
558 spherule layers shown in figure 4 does show some steepening at the larger impactor sizes.  
559 This disagreement between the main-belt SFD and spherule layer SFD shown in figure 4  
560 may be further indication that the population of ancient terrestrial impactors was  
561 something like Proposed SFD 1.

562

563 The blue “Proposed SFD 2” is main-belt like for impactors larger than 20 km in diameter  
564 and steeper than the main belt for impactors smaller than 30 km in diameter. If the E-  
565 belt had a significantly different collisional history than the main belt, this relative SFD  
566 could be consistent with the population of E-belt impactors (Bottke et al., 2015).  
567 However, the absolute E-belt flux would still be too low to explain the formation of the  
568 Archean spherule layers. “Proposed SFD 2” is similar to the SFD of asteroid families  
569 created by cratering on a large parent body (Durda et al., 2007). Because little is known  
570 about the initial SFD of giant impact ejecta, this SFD is also potentially consistent with  
571 giant impact ejecta (Jackson et al., 2014). Clearly, detailed modeling of the formation and  
572 collisional evolution of giant impact ejecta is required to determine if a giant impact  
573 ejecta origin for the LHB is consistent with constraints on the ancient impactor  
574 population.



575

576 **Figure 7:** Log-log plot of the cumulative number of impacts larger than a given size  
 577 plotted as a function of impactor diameter. The dashed red and black curves are the same  
 578 as those described in Figure 4 and represent the main-belt SFD. The black points with  
 579 error bars represent the SFD from spherule layers that formed between 3.2-3.5 Ga as  
 580 described in Figure 4. The grey diamonds show the relative number of impactors larger  
 581 than 70 km in diameter and 5.5 km in diameter needed to explain the lunar cratering  
 582 record. The blue squares show the same constraint but with a higher total flux.  
 583

584

585 The spherule record along with lunar cratering constraints based on the apparent lack of  
 586 mega-basins (Minton et al., 2015b) allow for a range of possible impactor SFDs (Figure  
 587 7). These SFDs, however, make completely different predictions for the number of  
 588 smaller craters we expect to find on the Moon. Fasset and Minton (2013) recently  
 589 compiled a variety of constraints based on the lunar cratering record (Neukum et al.,  
 590 2001; Stöffler and Ryder, 2001), putting them all in terms of the rate at which craters  
 591 larger than 20 km in diameter form on the Moon (Figure 8).

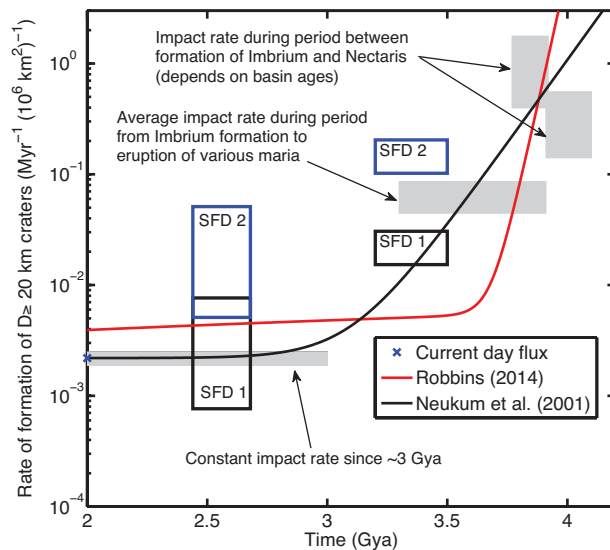
592

593 To compare the spherule layer record to the lunar cratering record, we first estimate the  
594 impactor size required to make a 20-km diameter crater. Using Equation 4 with lunar  
595 gravity  $g = 1.62 \text{ m/s}^2$  and  $D_{SC} = 15 \text{ km}$  appropriate for the Moon (Croft, 1985),  $v_{imp} =$   
596  $16 \text{ km/s}$  typical for the Moon (Yue et al., 2013),  $\rho_{imp} \approx \rho_{target}$ , and the most probable  
597 impact angle  $\theta = 45^\circ$ , we find a 1.1 km diameter impactor is required to make a 20 km  
598 diameter crater on the Moon. As shown in section 2, the spherule layers that formed  
599 between 2.44-2.8 Ga and 3.2-3.5 Ga are consistent with an impactor flux that is 1-10  
600 times and 20-40 times the current day flux, respectively, for very large impactors (~10-  
601 100 km in diameter). To estimate the flux of impactors larger than 1.1 km in diameter, we  
602 then extrapolate to smaller impactor sizes using proposed SFD 1 (black boxes) and  
603 proposed SFD 2 (blue boxes) (where proposed SFD 2 is assumed to be main-belt like for  
604 impactors smaller than 5.5 km in diameter).

605

606

607



608

609 **Figure 8:** Estimates of impactor flux on the Moon. The filled grey boxes are estimates  
 610 made by Fassett and Minton (2013). The blue star plotted at 2 Ga is the current impactor  
 611 flux according to observations of NEOs. The comparison of flux based on spherule layers  
 612 to lunar cratering record assumes that 17 impactors of a given size hit the Earth for every  
 613 one that hits the Moon (Bottke et al. 2012). The flux implied by the spherule layers is  
 614 estimated assuming proposed SFD 1 (black boxes) and proposed SFD 2 (blue boxes). The  
 615 red and black curves are best fit estimates from Neukum et al. (2001) and Robbins  
 616 (2014), respectively. The curves were scaled from the rate of formation of 1 km diameter  
 617 craters by normalizing to the current rate at which 20-km diameter craters form on the  
 618 Moon.  
 619

620 When using proposed SFD 1, the rate of formation of 20 km diameter craters is consistent  
 621 with the lunar crater chronology of Neukum et al. (2001) (Figure 8). Whereas, if we use  
 622 proposed SFD 2 the implied flux is roughly an order of magnitude higher than the  
 623 Neukum lunar cratering chronology (Figure 8). On this basis we argue that proposed  
 624 SFD 1 is more consistent with the lunar chronology than proposed SFD 2. Although  
 625 proposed SFD 1 does better than proposed SFD 2, neither SFD fits the chronology of  
 626 Robbins (Robbins, 2014). This may imply that the Neukum (2001) chronology is more  
 627 representative of the terrestrial impactor flux.

628

629 **5 Discussion:**

630 We note that the chronology of Robbins (2014) is in disagreement with the average rate  
631 of formation of 20-km diameter craters on the lunar maria (Figure 8, Fassett and Minton  
632 2013). Although, Robbins (2014) was careful to remove clusters of secondary craters,  
633 distant secondary craters may be spatially homogeneous (McEwen and Bierhaus, 2006).  
634 The only way to ensure secondary craters are omitted is to count only craters larger than  
635 ~1 km in diameter (McEwen and Bierhaus, 2006), but Robbins (2014) focuses on craters  
636 1 km in diameter and smaller. Consequently, we prefer the grey boxes in Figure 8 as  
637 constraints, as these flux estimates are based on the number of 20-km diameter craters  
638 (Fasset and Minton 2013). Clearly there are some significant uncertainties associated  
639 with interpretations of the lunar crater record.

640

641 The exceptional agreement between the current rate of formation of lunar craters larger  
642 than 20 km in diameter implied by observations of NEO's and estimates based on lunar  
643 craters provides an independent validation of the crater scaling laws discussed in section  
644 3 (Figure 8). Recent careful work interpreting the terrestrial cratering record by Hughes  
645 (2000) suggest craters larger than 20 km in diameter were created at a rate of  $(3.46 \pm$   
646  $0.30) \times 10^{-15} \text{ km}^{-2} \text{ yr}^{-1}$  over the past  $125 \pm 20$  Myr. This is in excellent agreement with  
647 crater scaling laws and estimates of the current day impactor flux based on observations  
648 of NEO's. Within the reported error, the commonly used  $(5.6 \pm 2.8) \times 10^{-15} \text{ km}^{-2} \text{ yr}^{-1}$   
649 (Grieve, 1998) for the formation rate of craters larger than 20 km in diameter is  
650 consistent with estimate of Hughes (2000).

651

652 Another potential source of error come from uncertainties in the estimates of the sizes of  
653 impactors that created the Archean spherule layers. Estimates based on layer thickness  
654 and extraterrestrial material content generally agree that the centimeters to 10's of  
655 centimeters thick Archean spherule layers were created by impactors that were ~10-90  
656 km in diameter (Johnson and Melosh, 2012b; Kyte et al., 2003; Lowe et al., 2003, 2014;  
657 Lowe and Byerly, 2015). However, estimates based on extraterrestrial material content  
658 may be affected by the heterogeneous distribution of Ni-rich chromium spinel which  
659 accounts for the bulk of the enrichment in platinum group elements. Additionally, many  
660 layers show signs of dilution, redeposition by surface processes, and tectonic deformation  
661 potentially affecting the thickness estimates reported in table 1 (Lowe et al., 2003). It is  
662 also possible that some of the layers are not global vapor plume layers but are more  
663 proximal ejecta like deposits from the Sudbury or Vredefort impacts (Cannon et al.,  
664 20010; Huber et al., 2014a,b). This has already been suggested for the Carawine,  
665 Jeerinah, and Dales Gorge spherule layers based on the characteristics of their spherules  
666 and related melt particles (Simonson et al., 2000; Jones-Zimberlin et al., 2006; Sweeney  
667 and Simonson, 2008). One test of the estimates of impactor size comes from the  
668 comparison to the lunar cratering record. For example, if the impactor flux implied by the  
669 Archean spherule layers was well above that implied by the lunar cratering record this  
670 may imply impactor sizes are consistently over estimated. Figure 8 shows that for a  
671 reasonable impactor size frequency distribution, it is possible to reconcile the impactor  
672 flux implied by spherule layers with flux estimates based on the lunar cratering record.

673



674 When an impactor component is recognized in a spherule layer, its composition can act  
675 as a further constraint on LHB models. The Chromium isotopes in S2, S3, and S4 (from  
676 3.2-3.5 Ga) all imply they were formed by carbonaceous chondrite impactors (Kyte et al.,  
677 2003). This is in contrast to the younger layers that formed between 2.44-2.68 Ga, which  
678 show a variety of compositions consistent with E-chondrites, Martian meteorites, or  
679 ordinary chondrites (Simonson et al., 2009). The compositions of the older layers, which  
680 imply an impactor flux ~20-40 the current impactor flux, may appear inconsistent with a  
681 giant impact origin for the LHB (Minton et al., 2015a; Volk and Gladman, 2015).  
682 However, if ejecta from a giant impact on Mars created the spherule layers, the common  
683 composition of S2, S3, and S4 could be explained by one of the bodies involved in the  
684 giant impact being a large carbonaceous chondrite, potentially a body similar to Ceres.

685

686 It is intriguing that the Martian moons, Phobos and Deimos, appear to be a combination  
687 of Martian and carbonaceous chondrite material (Citron et al., 2015). Moreover, Citron et  
688 al. (2015) suggest that Phobos and Deimos were the result of the putative Borealis-  
689 forming giant impact (Andrews-Hanna et al., 2008). The return of samples from Mars,  
690 Phobos, and Deimos along with detailed isotopic analysis could conceivably detect the  
691 signature of the putative giant impactor. Regardless of the source of the ancient  
692 impactors, the terrestrial spherule layers, when coupled with the lunar cratering record,  
693 clearly offer valuable clues about the population of ancient terrestrial impactors.

694

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